OU MATHDAY 2001 HIGHER ALGEBRA TEST

1. Solve this system of equations:

$$9x + 21y = -11$$

$$8x + 6y = -4/3$$

- (a) (5/3, 2/3); (b) (-1/3, -2/3); (c) (1/3, -2/3); (d) (-5/3, 2);

- (e) (5/3, -2).
- **2.** Find the solution set of $|2x 1| \ge 5$

- (a) $\{x : x \le 2\}$; (b) $\{x : x \ge 3\}$; (c) $\{x : x \le -2\} \cap \{x : x \ge 3\}$;
- (d) $\{x: x \le -2\} \cup \{x: x \ge 3\};$
- (e) The empty set.
- **3.** Find the simplest radical form of $3\sqrt{6} \cdot \sqrt{15}$
 - (a) $6\sqrt{10}$;
- **(b)** $27\sqrt{10}$; **(c)** $9\sqrt{10}$;
- (d) $12\sqrt{10}$;

- (e) None of these.
- **4.** Given the line whose equation is 2x 3y = 6. Where does the point P(-5, -6) lie?
 - (a) in the halfplane above the line
 - (b) in the halfplane below the line
 - (c) on the line
 - (d) all of the above
 - (e) none of the above
- 5. Which of the following describes the graph of the given set

$$\{(x,y): x^2 + y^2 \le 25\} \cap \{(x,y): x + y = -5\}$$

(a) a point; (b) a segment; (c) a ray; (d) a line; (e) none of these.

Typeset by $\mathcal{A}_{\mathcal{M}}\mathcal{S}$ -TEX

- **6.** Find the numerical coefficient of the term in x^4 in the expansion of $(x-2)^6$.
 - (a) 500; (b) 120; (c) 60; (d) 480; (e) none of these.
- 7. Simplify completely $\frac{a^2-7a+10}{a^2-2a-3} \div \frac{a-2}{a-3}$.
 - (a) -5; (b) 5; (c) $\frac{a-5}{a+1}$; (d) $\frac{a+5}{a+1}$; (e) none of these.
- **8.** If f is an even function then the graph of f is symmetric with respect to:
 - (a) the x-axis; (b) the y-axis; (c) the line y = x; (d) the line y = -x;
 - (e) cannot be determined.
- **9.** Simplify completely: $(3x^2 2x) (x^4 2x 1) + (5x^2 2)$.
 - (a) $-(x^4-8x^2+1)$; (b) $-x^4+8x^2-4x-3$; (c) $7x^2-1$; (d) x^4+8x^2+1 ;
 - (e) none of these.
- **10.** Which of the following is a false statement?
 - (a) $((-9)^2)^{1/3} = ((-9)^{1/3})^2$; (b) $((-2)^3)^{1/3} = ((-2)^{1/3})^3$;
 - (c) $((-9)^{1/2})^2 = ((-9)^2)^{1/2}$; (d) $((-16)^{-2})^{1/3} = ((-16)^{1/3})^{-2}$;
 - (e) $((-8)^2)^{1/3} = ((-8)^{1/3})^2$.
- 11. Find the inverse relation of y = (3/2)x 9
 - (a) y = (2/3)x + 18; (b) x = (2/3)y + 6; (c) y = (2/3)x + 6;
 - (d) 2y = 3x 18; (e) x = (3/2)y 9.
- **12.** If the distance from (2, b) to (-3, 5) is $\sqrt{74}$, find all possible values of b.
 - (a) $-2 \pm 2\sqrt{13}$; (b) $-5 \pm 3\sqrt{11}$; (c) $5 \pm 2\sqrt{73}$; (d) -2 or 12;
 - (e) 2 or 12.
- **13.** If x < 0, which of the following must be true?
 - (a) x 3 < 3x; (b) x 3 < 3 x; (c) $-3x < x^2$; (d) $x^3 > x + 3$;
 - (e) none of these.

14. Find the product of x and y if

$$(x+2y) + (4x-3y)\mathbf{i} = (2x-1) + (y-6)\mathbf{i}$$

- (a) 8; (b) 8; (c) -10; (d) 10; (e) 0.
- **15.** If $y = x^2$ and x increases from -5 to 5, then y will:
 - (a) increase; (b) decrease; (c) increase then decrease;
 - (d) decrease then increase; (e) remain constant.
- **16.** Solve: $\left| \frac{4p-1}{2} \right| < 6$.
 - (a) -1/2 ; (b) <math>-1 ; (c) <math>-13/4 ;
 - (d) -13/4 ; (e) <math>-11/4 .
- **17.** If x + y = 9 and y x = 7, find $x^2 + y^2$.
 - (a) 8; (b) 1; (c) 9; (d) 64; (e) 65.
- 18. The absolute value of the reciprocal of the difference of the reciprocals of two consecutive odd positive integers is 3/2. Find the sum of these two integers.
 - (a) 4; (b) 6; (c) 8; (d) 10; (e) the integers do not exist.
- **19.** A binomial factor of $b^3 + b^2 + b + 1$ is:
 - (a) b+1; (b) b-1; (c) b^2+10 ; (d) b^2-1 ; (e) b^2+2 .
- **20.** If 2y 6 varies directly as the square of x + 2 and inversely as z 3, and if y = 1 when x = 2 and z = 11, find y when x = 4 and z = 9.
 - (a) 3; (b) 2; (c) 9; (d) -12; (e) none of these.
- **21.** If x is a real number, then compare 1^{3x+1} and 1^{3x} .
 - (a) $1^{3x+1} > 1^{3x}$; (b) $1^{3x+1} < 1^{3x}$; (c) $1^{3x+1} = 1^{3x}$;
 - (d)none of the above; (e) cannot be determined from the information given.
- **22.** If $f(x) = x^4 + 2x^3 x^2 + cx + k$, f(-2) = 20 and f(2) = 24, find c k.
 - (a) -27; (b) -17; (c) 0; (d) 17; (e) 27.

- **23.** If $\frac{3}{2+\frac{x+3}{3}}=\frac{3}{4}$, then what is the value of x?
 - (a) 3; (b) 2; (c) 0; (d) 3; (e) 2.
- **24.** For which equation is the sum of its two solutions greater than their product?
 - (a) $x^2 7x + 12 = 0$; (b) $x^2 + 9x 10 = 0$; (c) $x^2 + 8x = 0$;
 - (d) $x^2 + 4 = 0$; (e) none of these.
- 25. If n is a rational number, which of the following must be rational numbers?
 - **I.** 100n; **III.** $\frac{n}{100}$; **III.** n + 100.
 - (a) I only; (b) I and II only; (c) II and III only; (d) I, II, and III;
 - (e) none of the choices.

MU ALPHA THETA HIGHER ALGEBRA TEST TIE BREAKERS

1. a, b and c are solutions of the equation $x^3 - 2x^2 - 5x + 6 = 0$. Find the value of $a^2b^2c + ab^2c^2 + a^2bc^2$.

A. -216; **B.** 30; **C.** 60; **D.** 66; **E.** none of these.

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2. Solve for x:

$$\log_3(x+1) + 2\log_9(3x-1) - 2\log_3(x+2) = 1$$